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Granular Gases

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Contents

I. Kinetic Theory and Hydrodynamics

Kinetic Theory of Granular Gases	3
<i>T.P.C. van Noije, M.H. Ernst</i>	
Free Cooling of Particles with Rotational Degrees of Freedom	31
<i>T. Aspelmeier, M. Huthmann, A. Zippelius</i>	
Hydrodynamic Transport Coefficients of Granular Gases	59
<i>J.J. Brey, D. Cubero</i>	
Granular Gases: Probing the Boundaries of Hydrodynamics ..	79
<i>I. Goldhirsch</i>	
Granular Gases with Impact-Velocity-Dependent Restitution Coefficient	100
<i>N.V. Brilliantov, T. Pöschel</i>	
Boundary Conditions for Collisional Grain Flows at Bumpy, Frictional Walls	125
<i>J.T. Jenkins</i>	
Diffusion Process in Two-Dimensional Granular Gases	140
<i>C. Henrique, G. Batrouni, D. Bideau</i>	

II. Collisions and One-Dimensional Models

Energy Loss and Aggregation Processes in Low Speed Collisions of Ice Particles Coated with Frosts or Methanol/Water Mixtures	153
<i>F. Bridges, K. Supulver, D.N.C. Lin</i>	
Contact Mechanics and Coefficients of Restitution	184
<i>C. Thornton, Z. Ning, C.-y. Wu, M. Nasrullah, L.-y. Li</i>	
Kinetic Theory for 1D Granular Gases	195
<i>R. Ramírez, P. Cordero</i>	
Chains of Viscoelastic Spheres	203
<i>T. Pöschel, N.V. Brilliantov</i>	

III. Vibrated Granular Media

- Experimental Studies of Vibro-fluidised Granular Beds** 215
R.D. Wildman, J.M. Huntley, J.-P. Hansen
- Pattern Formation in a Vibrated Granular Layer** 233
E. Clément, L. Labous
- Experimental Study
of a Granular Gas Fluidized by Vibrations** 244
É. Falcon, S. Fauve, C. Laroche
- Computer Simulation of Vertically Vibrated Granular Layers
in a Box with Sawtooth-Shaped Base** 254
Z. Farkas, A. Vukics, T. Vicsek
- Resonance Oscillations in Granular Gases** 266
A. Goldshtein, A. Alexeev, M. Shapiro

IV. Granular Astrophysics

- Dynamical Evolution of Viscous Discs. Astrophysical
Applications to the Formation of Planetary Systems
and to the Confinement of Planetary Rings and Arcs** 281
A. Brahic
- Numerical Simulations
of the Collisional Dynamics of Planetary Rings** 330
H. Salo
- Formation of Narrow Ringlets in Saturn's Rings** 350
J. Hänninen
- Granular Viscosity, Planetary Rings
and Inelastic Particle Collisions** 363
F. Spahn, O. Petzschmann, J. Schmidt, M. Sremčević, J.-M. Hertzsch

V. Towards Dense Granular Systems

- The Equation of State for Almost Elastic, Smooth,
Polydisperse Granular Gases for Arbitrary Density** 389
S. Luding, O. Strauß

**Experimental Observations of Non-equilibrium Distributions
and Transitions in a 2D Granular Gas** 410
J.S. Urbach, J.S. Olafsen

**Effect of Excluded Volume and Anisotropy
on Granular Statistics: “Fermi Statistics” and Condensation** .. 429
D.C. Hong

How Much Can We Simplify a System of Grains?..... 445
M. Müller, H.J. Herrmann

Author Index 457

Preface

“Granular Material” as a subject of physical research has a long standing history. Eminent scientists such as Coulomb, Faraday, Hagen, Huygens, Rayleigh, Reynolds, and others contributed to the body of research. Following the early days, however, the physical approach gave way to engineering disciplines. Among other reasons, the enormous advances in computing power rekindled the scientific interest of physicists. In the last decade large-scale simulations of granular systems have given new insights into the nature of granular materials – and continue to do so.

In the strict definition, “Granular Gases” are dilute granular systems, i.e., many-particle systems, in which the mean free path of the particles is much larger than the typical particle size. This condition implies that the duration of particle contacts is much shorter than the mean flight time. In contrast to molecular gases, in Granular Gases the particle collisions occur dissipatively, i.e., in each binary collision the particles lose part of the kinetic energy of their relative motion. The dissipation of kinetic energy causes a series of non-trivial effects, such as the formation of clusters and other spatial structures, non-Maxwellian velocity distributions, anomalous diffusion, correlations in the velocity field, characteristic shock waves, and others. In the dilute limit and with the assumption of weak dissipation the formal similarity of natural gases and Granular Gases allows us to also describe the latter using the powerful tools of classical Statistical Mechanics, Kinetics, and Hydrodynamics. Granular Gases provide, more than any other granular system, the possibility of conducting simultaneously experimental and theoretical studies and numerical simulations as well. Part I of the volume comprises rigorous theoretical results for the dilute limit.

Such theoretical descriptions of a Granular Gas as a many-particle system requires comprehensive understanding of the details of collisions of only two isolated grains. Without this knowledge it would be impossible to deduce the macroscopic properties of Granular Gases. The properties of binary collisions and simple one-dimensional models are the subject of Part II.

Part III contains experimental investigations of Granular Gases: In order to maintain a steady gaseous state under gravity conditions, the material has to be excited externally to balance the loss of kinetic energy due to inelastic particle collisions. Ideally, the energy feed would be homogeneous and isotropic throughout the system, which is certainly difficult to achieve in an experiment. For the experimental investigation of Granular Gases feeding energy by mechanical vibrations of the container has proven to be a good compromise – to date all earthborn experiments make use of vibrated containers.

Large-scale Granular Gases in steady state are found in astrophysical systems as discussed in Part IV. The rings around the outer planets of the Solar System have been intensively studied for centuries and lots of data exist from earthbound and missile observations. Although there are still many open questions, several aspects of the rich structure of planetary rings are well understood. Therefore, planetary rings offer a wide field for practical application of Granular Gas theory and may, thus, serve as test systems to validate theoretical results.

The last part (Part V) of the book is devoted to possible generalizations with respect to increased density. High-density Granular Gases, in a broader sense, can be defined as systems with instantaneous binary collisions, i.e., only by the condition that the contact duration is thought to be negligible and, hence, does not affect the overall properties of the many-particle system. From the theoretical point of view this definition is more problematic since the assumption of Molecular Chaos as a prerequisite of simple kinetic theory may be violated. Nevertheless, many interesting phenomena occur in systems of increased density and there is a need to thus generalize the theory. The motivation for extending the gas picture to higher density is to bridge the still-existing gap between Kinetic Theory and fluid dynamics approaches, which are very successfully applied in engineering.

The articles in this volume are selected contributions of the conference “Granular Gases” held from March 8 to 12, 1999 in Bad Honnef. Many of the authors are renowned experts in the field and have decisively shaped the present state of knowledge. Therefore, the articles in this volume cover a large part of the present knowledge about Granular Gases, ranging from investigations of two-particle interactions to Kinetic Theory of dilute many-particle systems and numerical simulations of rather dense systems.

In order to find a wide readership not only among experts, but also among undergraduate and graduate students, the authors have been asked to present their material in a self-contained and pedagogical way. All contributions have been carefully refereed.

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